

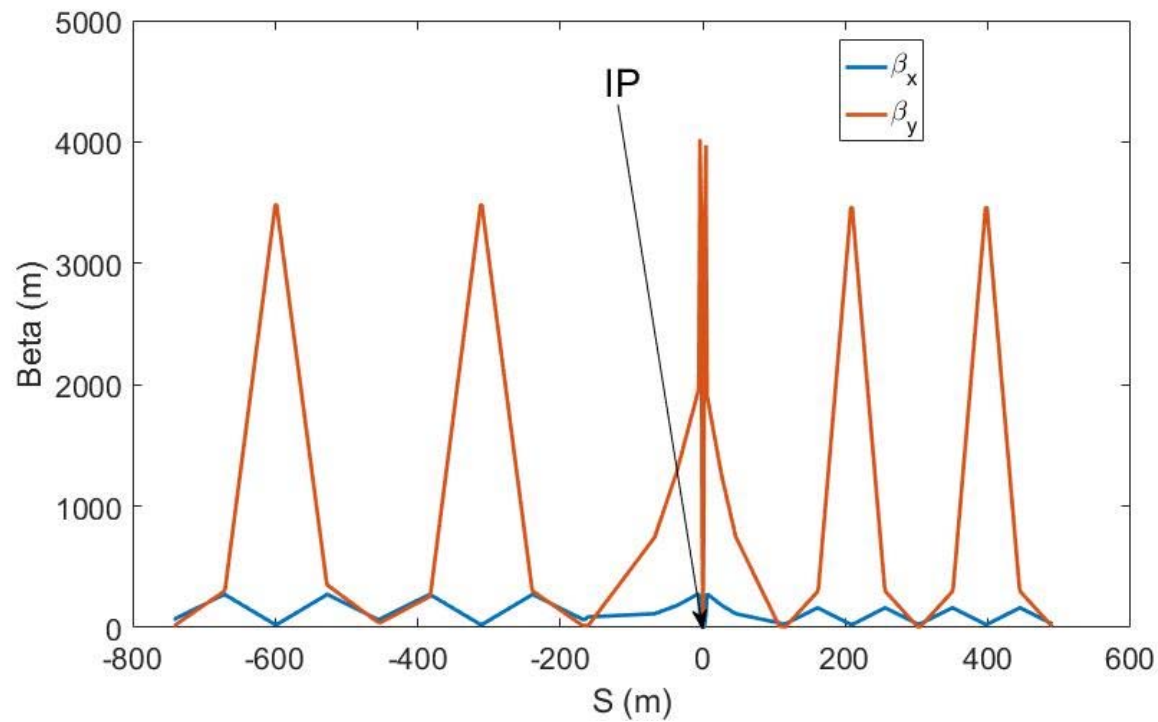
# Imperfection and correction for CEPC

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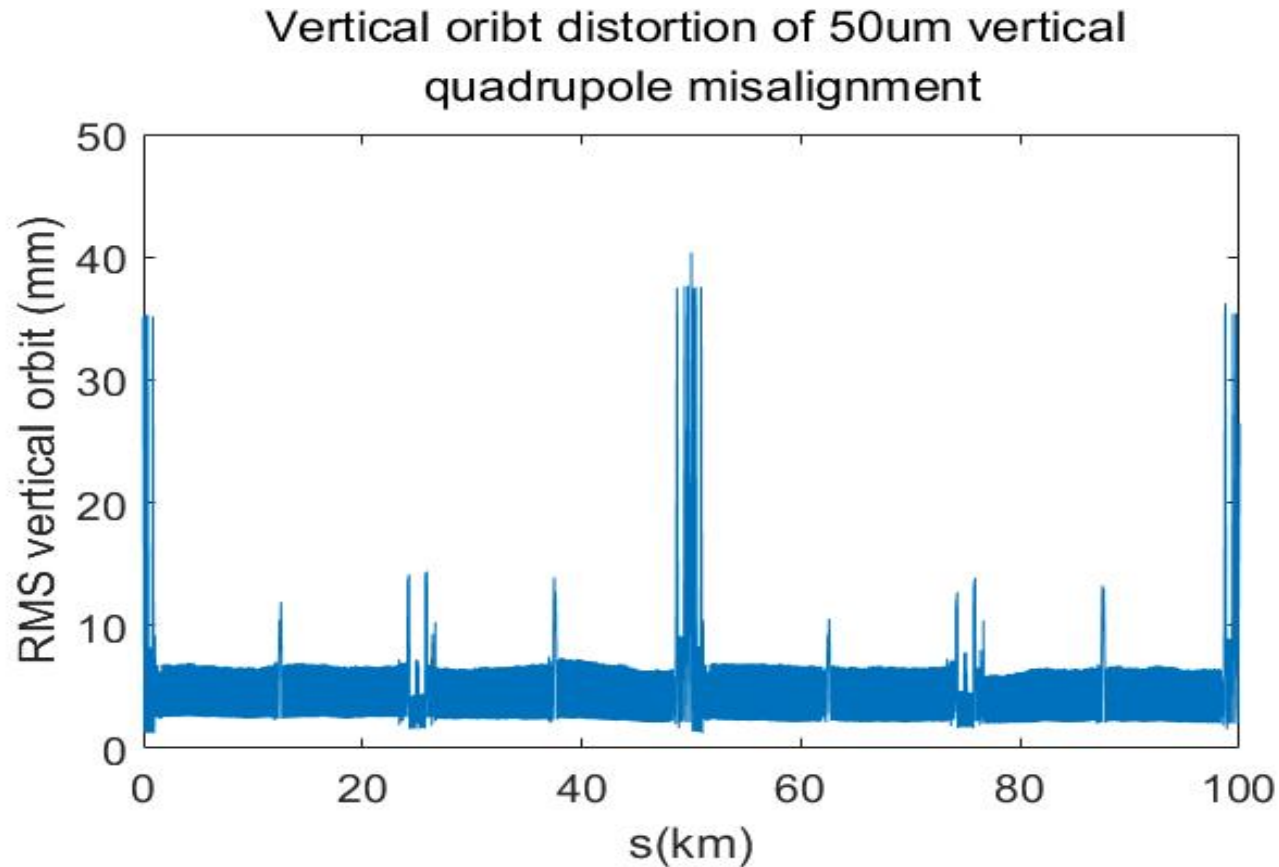
**IAS, 21-24 Jan 2019, Hong Kong**

# Lattice



- $E=120\text{GeV}$
- $v_x=363.11$   
 $v_y=365.22$
- $\beta_x^* = 0.36\text{m}$   
 $\beta_y^* = 0.0015\text{m}$   
 $\beta_{x,max}=599\text{m}$   
 $\beta_{y,max}=4023\text{m}$
- $\varepsilon_x = 1.21\text{nm}$   
 $\varepsilon_y = 2.4\text{pm}$

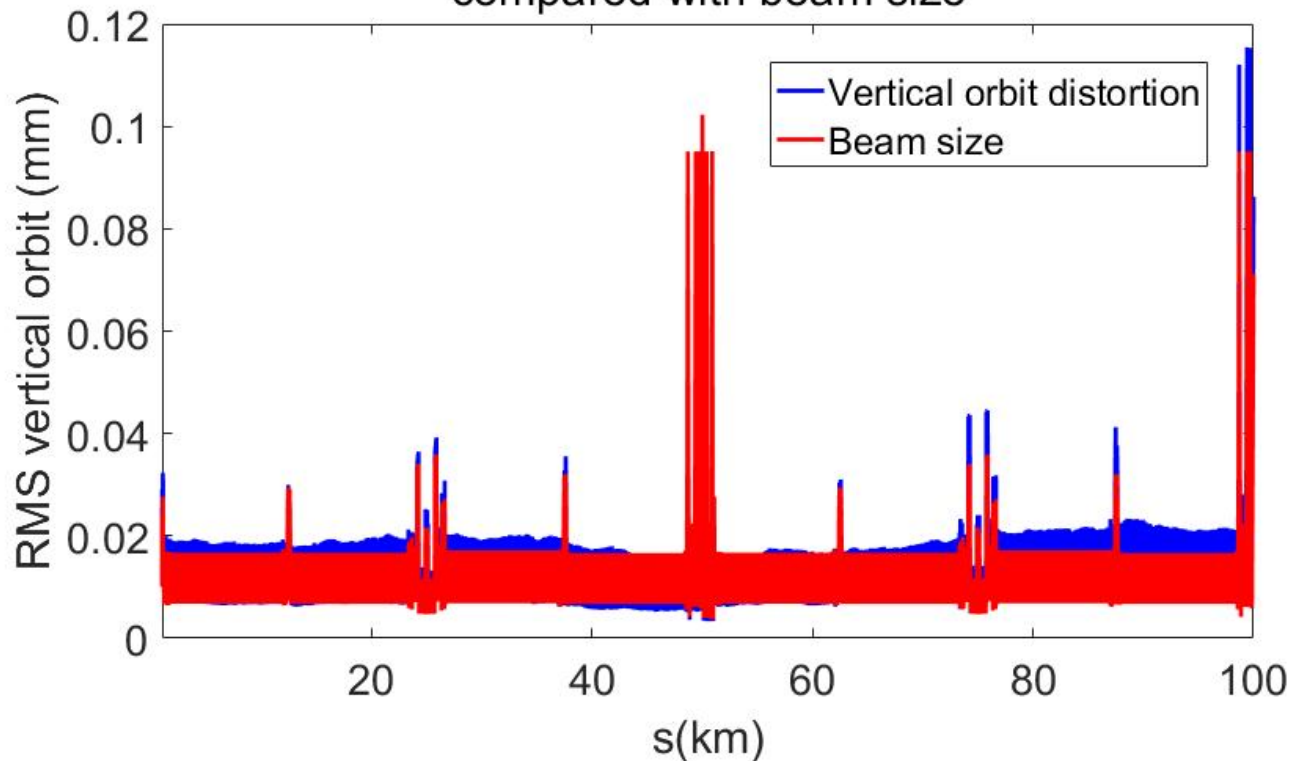
# Orbit amplification factor



- $\langle \Delta y_{\text{rms}} \rangle = 4.69\text{mm}$
- Orbit amplification factor =  $4.69/50\text{e-}3 = 94$
- Turn off sextupoles and FF is left perfectly aligned.

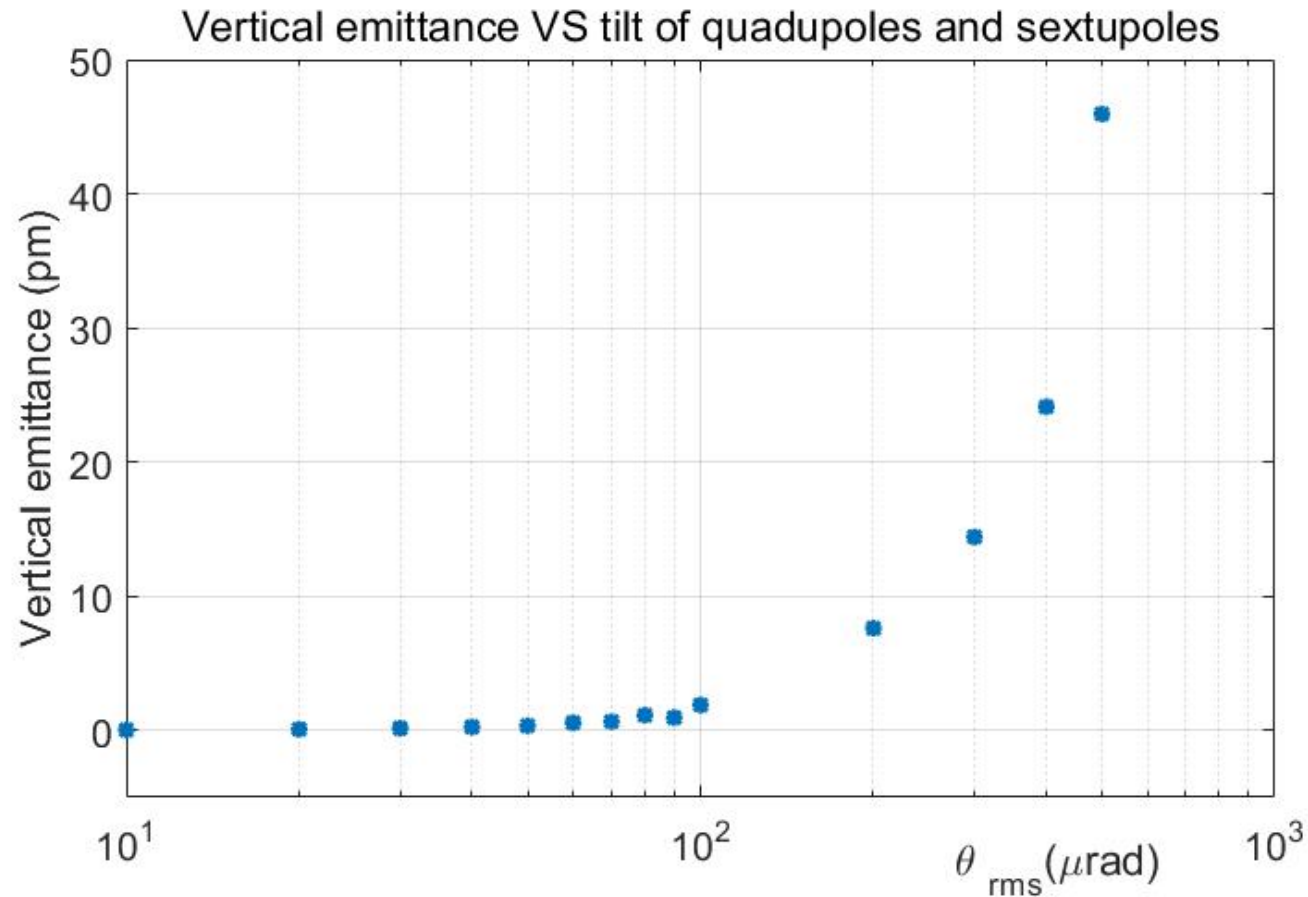
# Quadrupole jitter sensitivity

Quadrupole jitter caused vertical orbit distortion  
compared with beam size



- The RMS vertical orbit distortion caused by  $0.15\mu\text{m}$  quadrupole jitter is equal to beam size at 2.4pm vertical emittance.
- Turn off sextupoles and FF is left perfectly aligned.

# Quadrupoles and sextupoles tilt sensitivity



● 100  $\mu\text{rad}$  rotation  $\sim$  2pm vertical emittance

# Misalignment sensitivity

|                                                   | <b>Super <i>B</i><br/>LER</b> | <b>Super <i>B</i><br/>HER</b> | <b>ILC<br/>DRs</b> | <b>KEK<br/>ATF</b> | <b>CEPC</b>               |
|---------------------------------------------------|-------------------------------|-------------------------------|--------------------|--------------------|---------------------------|
| Vertical emittance (pm)                           | 4                             | 4                             | 2                  | 4.5                | 2.4 (0.2% coupling)       |
| Orbit amplification factor                        | 46                            | 44                            | 32                 | 21                 | 94                        |
| Quadrupole jitter sensitivity (nm)                | 209                           | 217                           | 221                | 227                | 150                       |
| Sextupole alignment sensitivity ( $\mu\text{m}$ ) | 95                            | 87                            | 70                 | 50                 | 16                        |
| Quadrupole tilt sensitivity ( $\mu\text{rad}$ )   | 166                           | 183                           | 79                 | 800                | 100 (sextupoles included) |

# Misalignment and field errors

| Component            | $\Delta x$ ( $\mu\text{m}$ ) | $\Delta y$ ( $\mu\text{m}$ ) | $\Delta\theta_z$ ( $\mu\text{rad}$ ) |
|----------------------|------------------------------|------------------------------|--------------------------------------|
| Arc quadrupole       | 100                          | 100                          | 100                                  |
| IR Quadrupole w/o FF | 50                           | 50                           | 50                                   |
| Sextupole            | 100                          | 100                          | 100                                  |

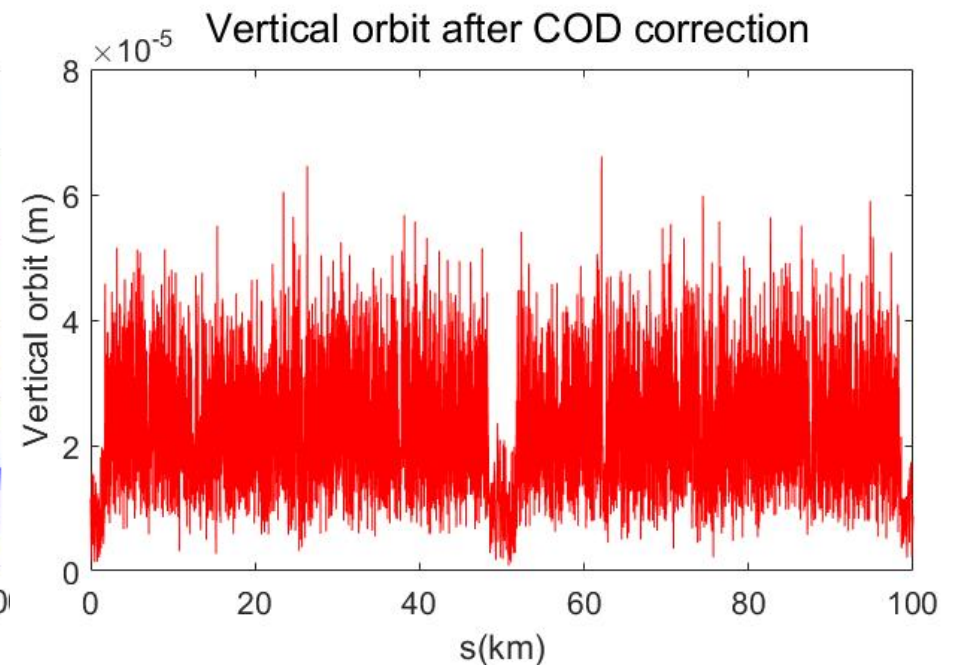
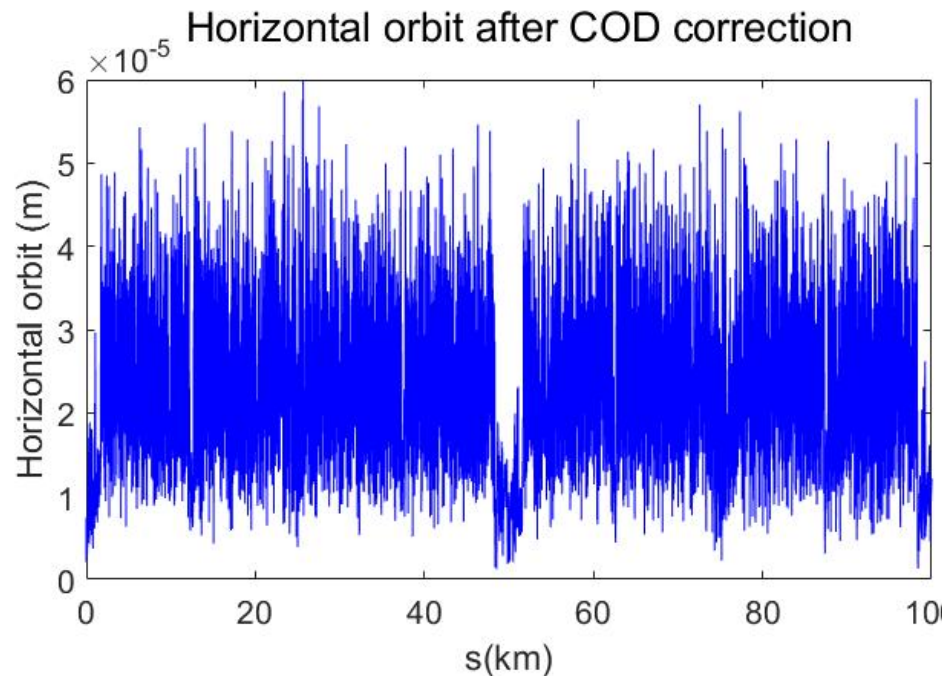
| Component      | Field error |
|----------------|-------------|
| Dipole         | 0.01%       |
| Arc Quadrupole | 0.02%       |

# Correction scheme

- COD correction with **sextupoles off** (the misalignment of FF is not included)
- **Turn on the sextupoles** and perform COD correction again.
- Dispersion correction (DFS)
- Beta beating correction (LOCO)
- Coupling and vertical dispersion correction (Local coupling parameter correction) .

# COD after correction

- BPMs placed at quadrupoles ( $\sim 1500$ , 4 per betatron wave)
- Horizontal correctors placed beside focusing quadrupoles ( $\sim 1500$ )
- Vertical correctors placed beside defocusing quadrupoles ( $\sim 1500$ )



Distortion  $\text{RMS}_{\text{COD}} < 0.1 \text{ mm}$  after orbit correction

# Dispersion correction

- **Dispersion free steering principle (DFS):** orbit manipulation by knob correctors.

$$\vec{d} = \begin{pmatrix} (1 - \alpha)\vec{u} \\ \alpha\vec{D}_u \end{pmatrix} \quad M = \begin{pmatrix} (1 - \alpha)A \\ \alpha B \end{pmatrix}$$

$$\vec{d} + M\vec{\theta} = 0$$

$\vec{u}$ : Orbit vector

$\vec{D}_u$ : Dispersion vector

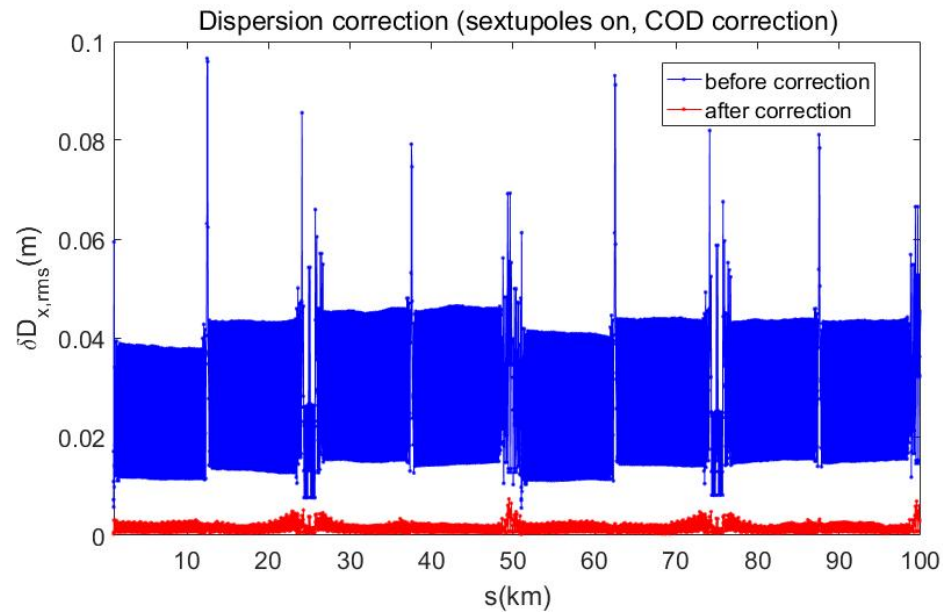
$\vec{\theta}$ : Corrector strengths vector

$\alpha$ : Weight factor

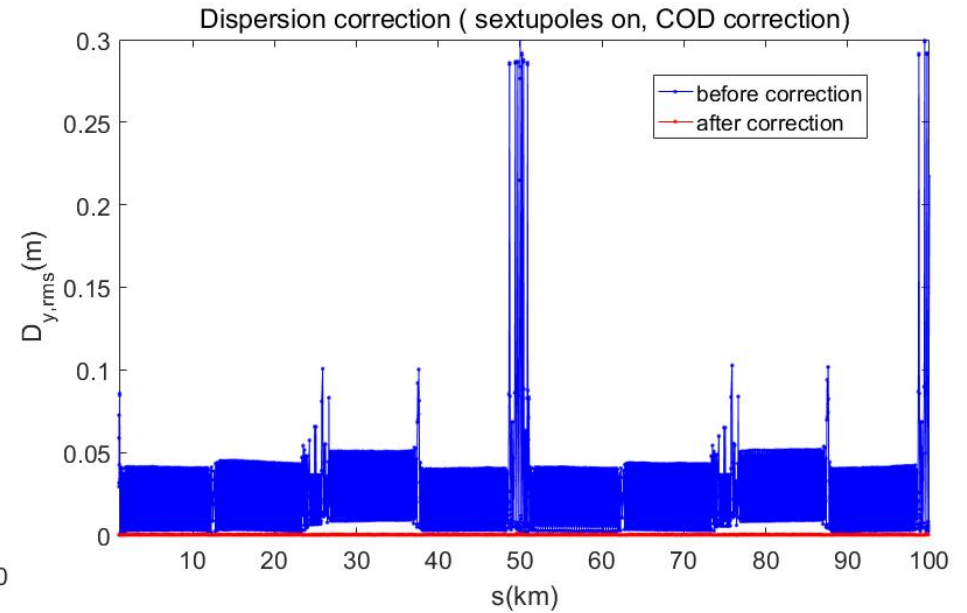
$A$ : Orbit response matrix

$B$ : Dispersion response matrix

# Dispersion correction



$\Delta D_{x,rms}$  decreased from 30mm to 1.7mm  
Factor 20 improvement



$D_{y,rms}$  decreased from 40mm to 0.2mm  
Factor 200 improvement

# Beta-beating correction

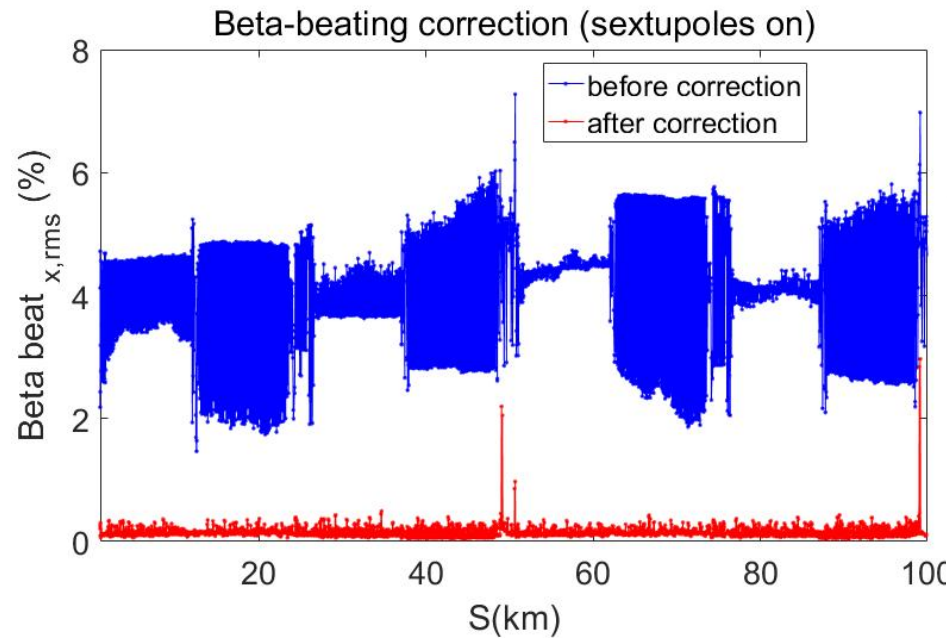
- Based on AT LOCO: model based correction
  - Establish lattice model  $M_{mod}$ , multi-parameter fit to the orbit response matrix  $M_{meas}$  to obtain calibrated model:

$$\chi^2 = \sum_{i,j} \frac{(M_{mod,ij} - M_{meas,ij})^2}{\sigma_i^2} \equiv \sum_{i,j} V_{ij}^2$$

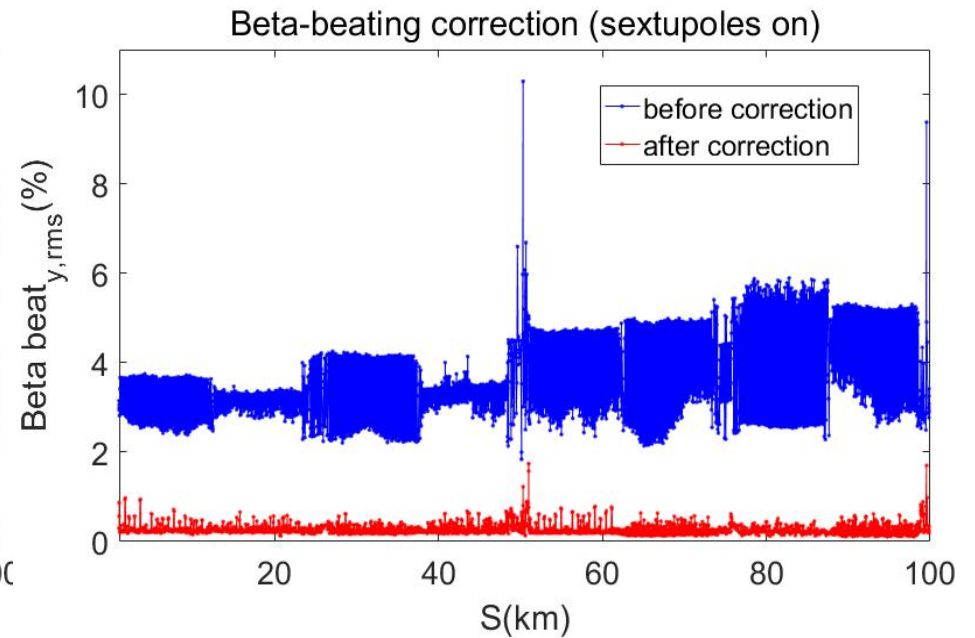
- Parameters fitted: K, KS ...
- Use calibrated model to perform correction and apply to machine.
- Application to correct beta-beating, dispersion and coupled response matrix.

# Beta-beating correction

- 1/5 quadrupole (~600 out of 3000 quadrupoles) strengths are changed to restore beta functions along the ring.



$\Delta\beta/\beta_{x,rms}$  decreased from 3.1% to 0.25%



$\Delta\beta/\beta_{y,rms}$  decreased from 3.7% to 0.3%

# Coupling correction

- Neglecting beam-beam effects

$$\varepsilon_y \simeq \varepsilon_{y0} + \kappa \varepsilon_x + rE^2(D_y^{\text{rms}})^2$$

- Local coupling parameter matching was developed for BEPCII.
- Both coupling and dispersion can be corrected.
- Using the trim coils of the sextupoles (~1000), which providing skew-quadrupole field, to perform emittance tuning for CEPC.
- The vertical orbit distortion due to a horizontal deflection at a BPM is:

$$\frac{\Delta y_{cod}}{\Delta x_{cod}} = \bar{c}_{b,22}k_1 + \bar{c}_{b,12}k_2 + \bar{c}_{c,11}k_3 + \bar{c}_{c,12}k_4$$

$k_1, k_2, k_3, k_4$  : only related to the decoupled linear optics

$\bar{c}_{b,22}, \bar{c}_{b,12}, \bar{c}_{c,11}, \bar{c}_{c,12}$ : local coupling parameters

$$\bar{c}_{b,12} = M_c \vec{k}_s$$

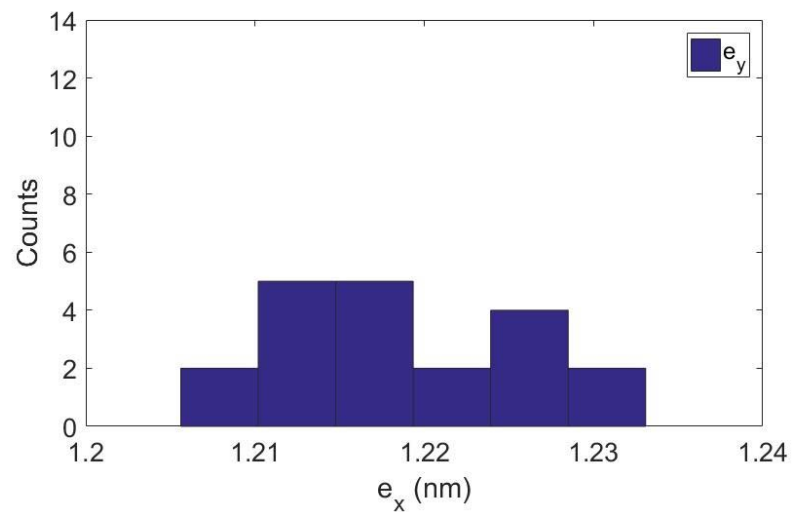
$M_c$ :  $\bar{c}_{b,12}$  response matrix

$\vec{k}_s$  : skew-quadrupole vector

# Emittance tuning

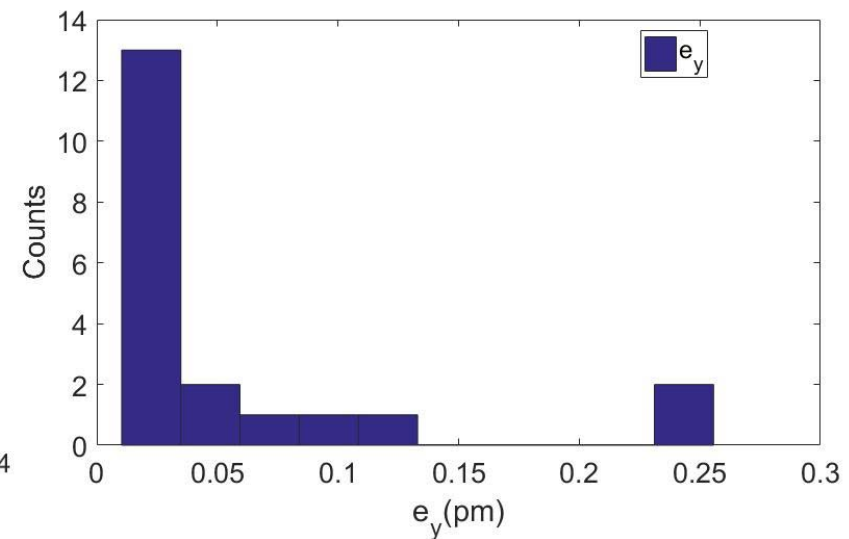
| Component            | $\Delta x$ (um) | $\Delta y$ (um) | $\Delta \theta_z$ (urad) |
|----------------------|-----------------|-----------------|--------------------------|
| Arc quadrupole       | 100             | 100             | 100                      |
| IR Quadrupole w/o FF | 50              | 50              | 50                       |
| Sextupole            | 100             | 100             | 100                      |

| Component      | Field error |
|----------------|-------------|
| Dipole         | 0.01%       |
| Arc Quadrupole | 0.02%       |



$$\epsilon_x = 1.22 \pm 0.008 \text{ nm}$$

$$\epsilon_y / \epsilon_x = 0.007 \%$$

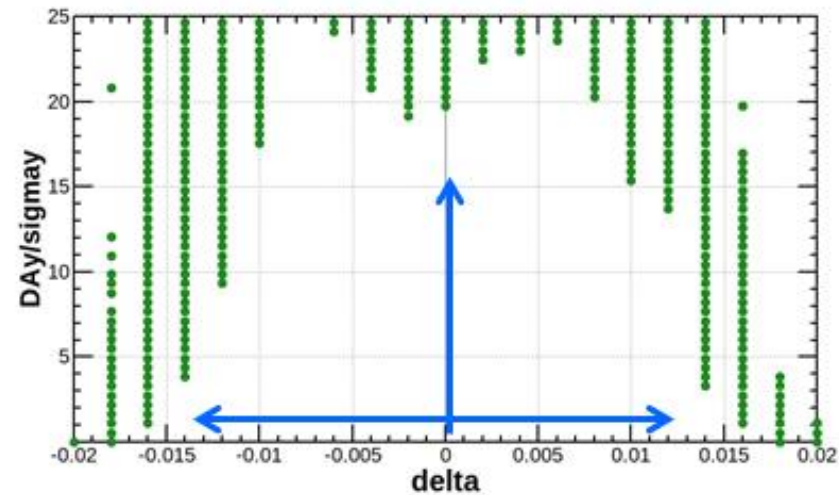
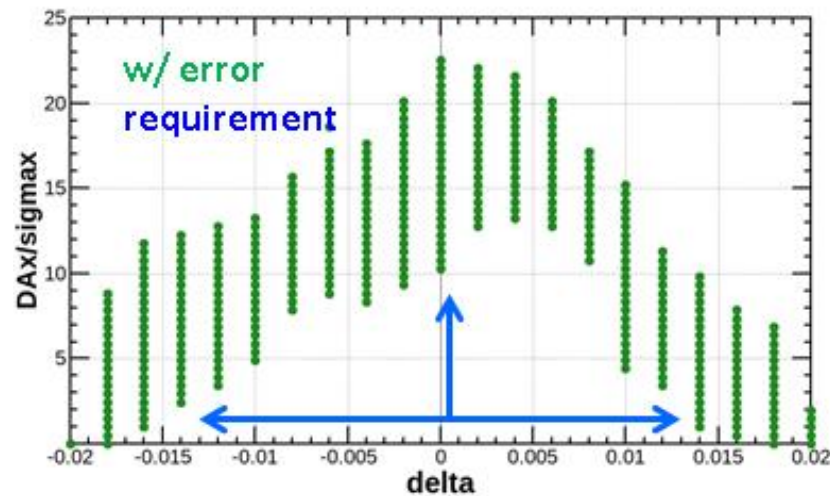


$$\epsilon_y = 0.09 \pm 0.07 \text{ pm}$$

# DA and MA

| Component            | $\Delta x$ (um) | $\Delta y$ (um) | $\Delta\theta_z$ (urad) |
|----------------------|-----------------|-----------------|-------------------------|
| Arc quadrupole       | 100             | 100             | 100                     |
| IR Quadrupole w/o FF | 50              | 50              | 50                      |
| Sextupole            | 100             | 100             | 100                     |

| Component      | Field error |
|----------------|-------------|
| Dipole         | 0.01%       |
| Arc Quadrupole | 0.02%       |



Requirement with on-axis injection  $8\sigma_x \times 15\sigma_y$  & 0.0135

Tracking done by Y.W.Wang

# Conclusions

- CEPC lattice is sensitive to the imperfections. Therefore, the optics correction is very challenging.
- CEPC optics correction procedure was demonstrated to be effective.
- With the abovementioned imperfections, both DA and MA after correction are acceptable.

# Towards TDR

- Study whether the tolerance of the imperfections can be relaxed.
- Optimize the correction strategy to achieve finer tuning of optics.
- Include imperfection of final focus (FF) quadrupoles.
- Include more types of imperfections.

*Thanks for you attention*